

28.9 Since the electrical force supplies the centripetal acceleration,

$$\frac{m_e v_n^2}{r_n} = \frac{k_e e^2}{r_n^2} \text{ or } v_n^2 = \frac{k_e e^2}{m_e r_n}$$

From $L_n = m_e r_n v_n = n\hbar$, we have $r_n = \frac{n\hbar}{m_e v_n}$, so

$$v_n^2 = \frac{k_e e^2}{m_e} \left(\frac{m_e v_n}{n\hbar} \right) \text{ which reduces to } \boxed{v_n = \frac{k_e e^2}{n\hbar}}$$

29.19 Recall that the activity of a radioactive sample is directly proportional to the number of radioactive nuclei present, and hence, to the mass of the radioactive material present.

$$\text{Thus, } \frac{R}{R_0} = \frac{N}{N_0} = \frac{m}{m_0} = \frac{0.25 \times 10^{-3} \text{ g}}{1.0 \times 10^{-3} \text{ g}} = 0.25 \quad \text{when } t = 2.0 \text{ h}$$

$$\text{From } R = R_0 e^{-\lambda t}, \text{ we obtain } 0.25 = e^{-\lambda(2.0 \text{ h})} \quad \text{and} \quad \lambda = -\frac{\ln(0.25)}{2.0 \text{ h}} = 0.693 \text{ h}^{-1}$$

$$\text{Then, the half-life is } T_{1/2} = \frac{\ln 2}{\lambda} = \frac{\ln 2}{0.693 \text{ h}^{-1}} = \boxed{1.0 \text{ h}}$$

29.22 Using $R = R_0 e^{-\lambda t}$, with $R/R_0 = 0.125$, gives $\lambda t = -\ln(R/R_0)$

or
$$t = -\frac{\ln(R/R_0)}{\lambda} = -T_{1/2} \left[\frac{\ln(R/R_0)}{\ln 2} \right] = -(5730 \text{ yr}) \left[\frac{\ln(0.125)}{\ln 2} \right] = \boxed{1.72 \times 10^4 \text{ yr}}$$

