

26.17 The momentum of the electron is

$$p_e = \gamma m_e v = \frac{(9.11 \times 10^{-31} \text{ kg})(0.90c)}{\sqrt{1 - (0.90)^2}} = (1.9 \times 10^{-30} \text{ kg})c$$

If the proton has the same momentum, then

$$p_p = \gamma m_p v = \frac{(1.67 \times 10^{-27} \text{ kg})v}{\sqrt{1 - (v/c)^2}} = (1.9 \times 10^{-30} \text{ kg})c$$

which reduces to  $(8.9 \times 10^2)(v/c) = \sqrt{1 - (v/c)^2}$  and yields

$$v = (1.1 \times 10^{-3})c = (1.1 \times 10^{-3})(3.0 \times 10^8 \text{ m/s}) = \boxed{3.3 \times 10^5 \text{ m/s}}$$

$$26.28 \quad (a) \quad E_R = mc^2 = (1.67 \times 10^{-27} \text{ kg})(3.00 \times 10^8 \text{ m/s})^2 \left( \frac{1 \text{ MeV}}{1.60 \times 10^{-13} \text{ J}} \right) = \boxed{939 \text{ MeV}}$$

$$(b) \quad E = \gamma mc^2 = \gamma E_R = \frac{E_R}{\sqrt{1 - (v/c)^2}}$$

$$= \frac{939 \text{ MeV}}{\sqrt{1 - (0.950)^2}} = 3.01 \times 10^3 \text{ MeV} = \boxed{3.01 \text{ GeV}}$$

$$(c) \quad KE = E - E_R = 3.01 \times 10^3 \text{ MeV} - 939 \text{ MeV} = 2.07 \times 10^3 \text{ MeV} = \boxed{2.07 \text{ GeV}}$$

$$26.39 \quad KE = E - E_R = (\gamma - 1)E_R$$

$$\text{so} \quad \gamma = 1 + \frac{KE}{E_R} = \frac{1}{\sqrt{1 - (v/c)^2}} \quad \text{giving} \quad v = c \sqrt{1 - \frac{1}{(1 + KE/E_R)^2}}$$

(a) When  $KE = q(\Delta V) = e(500 \text{ V}) = 500 \text{ eV}$ , and  $E_R = 939 \text{ MeV}$ , this yields

$$v = c \sqrt{1 - \frac{1}{\left[1 + 500 \text{ eV}/(939 \times 10^6 \text{ eV})\right]^2}} = 1.03 \times 10^{-3} c = \boxed{3.10 \times 10^5 \text{ m/s}}$$

(b) When  $KE = q(\Delta V) = e(5.00 \times 10^8 \text{ V}) = 500 \text{ MeV}$

$$v = c \sqrt{1 - \frac{1}{(1 + 500 \text{ MeV}/939 \text{ MeV})^2}} = \boxed{0.758c}$$

**26.40** From  $E^2 = (pc)^2 + E_R^2$  with  $E = 5E_R$ , we find that  $p = \frac{E_R \sqrt{24}}{c}$

(a) For an electron,  $p = \frac{(0.511 \text{ MeV})\sqrt{24}}{c} = \boxed{2.50 \text{ MeV}/c}$

(b) For a proton,  $p = \frac{(939 \text{ MeV})\sqrt{24}}{c} = 4.60 \times 10^3 \frac{\text{MeV}}{c} = \boxed{4.60 \text{ GeV}/c}$